Experimental Tests on Orthotropically RC Rectangular Slabs Having Various Restrained Edges and Subjected to Uniform Load

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Abstract

In this research, nine orthotropically reinforced concrete (RC) rectangular slabs having various boundary restraints at the edges are tested under uniformly distributed load. The main aim of these tests is to show that when some or all edges of a slab are restrained against rotation and horizontal translation the ultimate load carrying capacity of the slab will be enhanced greatly above that suggested by the simple Johansen’s yield line theory (1). For this purpose, a specially designed rig is constructed and used for providing slabs with various boundary restraints along their edges.

The results of tests, which are presented in the form of load-deflection curves plotted non-dimensionally, show that for restrained slabs the enhancement in load above Johansen’s load ranges between 50% and 100% depending on the number and positions of the slab restrained edges. These results are also used to examine the accuracy of a recently submitted elastic-plastic theoretical model (2).

Keywords: experimental test; orthotropic; reinforced concrete; slab

Notations

- **d**: Effective depth of slab,
- **\( f_c \)**: Specified compressive strength of concrete by cylinder test (MPa),
- **\( f_y \)**: Yield stress of steel reinforcement (MPa),
- **h**: Overall depth of slab,
- **\( l_b \)**: Long span of rectangular slab,
- **\( l_s \)**: Short span of rectangular slab,
- **q**: Uniformly distributed load per unit area,

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q<sub>u</sub>, Ultimate uniformly distributed load per unit area given by Johansen's yield line theory.

w, Vertical deflection at centre of slab, and

ρ, Ratio of steel area to effective area of concrete = A<sub>s</sub>/d.

**Introduction**

The phenomenon of membrane action in RC slabs was mainly introduced by Ockleston<sup>(3)</sup> in his prototype test on a dental hospital building in Johannesburg, Powell<sup>(4)</sup> in his Ph.D thesis and Wood<sup>(5)</sup> in his famous book. They confirmed experimentally and analytically that when the edges of the slab are restrained against rotation and horizontal translation, membrane action will be developed in the slab which enables the slab to carry load far beyond that predicted by Johansen's yield line theory. Many researchers, thereafter, such as Christiansen<sup>(6)</sup>, Park<sup>(7,8)</sup>, Sawczuk and Winnicki<sup>(9)</sup>, Maher<sup>(10)</sup>, Roberts<sup>(11)</sup>, Datta and Ramesh<sup>(12)</sup>, Desai and Kulkarni<sup>(13)</sup>, Al-Hassani<sup>(14)</sup>, Ouyang and Swarts<sup>(15)</sup>, Rankin et al<sup>(16)</sup>, and some others reported experimental ultimate loads of restrained slab models that were extraordinarily large. However, in the majority of these tests the slabs were considered to be either partially restrained against longitudinal expansion or fully restrained against rotation and lateral movement.

Since the present of restraining condition at some or all edges of a RC slab can affect its flexural performance, it is aimed from the present research to provide experimental data on the tests of RC rectangular slabs having the nine possible boundary condition cases shown in Figure (1).

**Experimental Work**

Nine concrete rectangular slabs having orthotropic reinforcement in the two directions and different boundary restraints were cast and tested under uniform load to obtain actual load-deflection curves for such slabs. All the slab models were rectangular of size 1100*750*25 mm but when placed over supports gave clear spans of 900*550 mm. A concrete mix of (1:1.75:2) with water/cement ratio of (0.52) was used in all slab models. The slab models were reinforced with 2.6 mm diameter smooth steel wires. Three specimens of these wires were tested under direct tension by using the tensile testing machine available in the laboratory of the Department of Minerals and Production Engineering in the University of Technology, (Photo 1). The test gave an average tensile yield stress of the three steel wires of 396 MPa and their idealized average stress-strain relationship is shown in Figure (2).

**Details Of The Test Slabs.**

Each test slab was orthotropically reinforced with 2.6 mm diameter steel wires in the two orthogonal directions. The steel wires were placed at the bottom face of the slab in the positive moment regions occurring at the slab central area and at the top face of the slab in the negative moment regions adjacent to fixed supports. Figure (3) shows the notations used for the steel ratios at different locations in the slab. The reinforcement running in the short direction of the slab had a 5 mm concrete cover. The ratio of steel reinforcement provided in the short span was (ρ<sub>a</sub><sup>+</sup>=0.36%) for positive moment region and (ρ<sub>a</sub><sup>-</sup>=0.72%) for negative moment regions if present. In the long direction, the ratio of steel reinforcement was (ρ<sub>b</sub><sup>+</sup>=0.26%) for positive moment region and (ρ<sub>b</sub><sup>-</sup>=0.52%) for negative moment regions if present. The details of the nine test slabs are shown in Table (1). It can be seen from this table that all steel ratios were carefully designed and computed to be larger than the minimum value for shrinkage and temperature required by ACI-05 code<sup>(17)</sup>.
Casting And Curing.
Having constructed the specimen's mould, the reinforcing steel wires were orthotropically arranged along the two orthogonal directions of the mould and carefully placed in position by using tying wires. In order to get a constant clear cover, small pieces of steel wires having 5 mm diameter were placed under the bottom layer of the reinforcement mesh. Photos (2) to (7) show the pattern of the reinforcement mesh used in some cases of the test slabs.

Mixing of materials was performed in accordance to ASTM C 192\textsuperscript{(18)}. The procedure used involved first, adding all the aggregate into the mixer with half the quantity of water, mixing for a short time then adding the remaining ingredient of cement followed by the remaining water quantity. The components were then mixed for a period of five minutes. This procedure yielded a well mixed concrete.

To assess the compressive strength of concrete, three steel cylindrical moulds having 100 mm diameter and 200 mm height were used to cast the concrete control specimens according to ASTM C39\textsuperscript{-86}\textsuperscript{(19)}. The three cylinders of control specimens were also oiled and prepared. Thus a system of a slab mould and three control cylinders were placed on a table vibrator. After the concrete had been mixed, casting was carefully performed. The vibrator was switched on for a small period till a perfect concrete compaction was achieved, and the slab surface was then carefully leveled.

After one day curing by means of wet jute sacks, the slab model and the three control concrete cylinders were stripped off their moulds and covered by wet jute sacks for 28 days before exposing to normal weather condition to get a surface dry condition then the slab and the control specimens were tested. The three control concrete cylinders were tested under direct axial compression to get the concrete compressive strength ($f'_c$). An average result of three specimens was adopted for each test as listed in Table (1).

The Testing Rig And The Restraining Requirements At The Slab Edges.
A slab to be tested was supported on a stiff rectangular frame fabricated from steel. Photo (8) shows a RC rectangular slab fixed along three edges while the fourth long edge is simply supported (slab case 8).

To achieve a fixed edge in a slab model (represented by end condition 1 in Figure 4), a steel channel was placed on the top face of the slab at that edge which was tightened firmly to the slab by using 12.7 mm diameter steel bolts. The number of steel bolts used to fix a long and a short edge in a slab model was 4 and 3 respectively (see Photo 8) and they were positioned such that one steel bolt was used at each corner of the slab to prevent it from any possible uplift during the slab loading process in additions to two more bolts in a long fixed edge and one "central" bolt in a short fixed edge. A steel plate was also used at each fixed edge which was tightened to the edge by using horizontal steel screws to prevent any possible lateral movement of that edge.

A simply supported edge in a slab model (represented by end condition 2 in Figure 4) was achieved by simply placing the slab over a steel plate connected to the testing frame through welding, and without using any vertical bolts or horizontal screws so that the edge was free to rotate and move horizontally.

System Of Loading And Testing Procedure.
Uniformly distributed load is the most common load encountered in practice. In the laboratory such load can be produced by using a large number of point loads applied through hydraulic jacks, for example Wood\textsuperscript{(5)} used 16 point loads which were distributed uniformly over the entire surface of the slab to represent uniform loading, while Johansen\textsuperscript{(1)} used
24 point loads to obtain uniformly distributed load (UDL). Alternatively hydrostatic or pneumatic pressure can be applied on a test slab as used by Hayes\cite{20}, while Sawczuk and Winnicki\cite{9} and Park\cite{7,8} achieved UDL by applying water pressure to the bottom face of the slab. The uniform load can somehow be produced using sand as was adopted by Al-Shadidi\cite{21} and Hassan\cite{22}.

In this research, the uniform load was furnished as follows
\begin{itemize}
  \item[i)] Using one layer of 50 mm diameter steel ball distributed uniformly over the entire surface of the slab which were held in position by using a steel box placed on the slab directly over the supports (as shown in Figure 5)
  \item[ii)] More load was applied using small sacks of sand distributed uniformly over the layer of steel balls.
  \item[iii)] In cases of restrained slabs, additional load was added on the slab using fragments of steel distributed over the sacks of sand.
\end{itemize}

It is to be noted that the steel box placed on the slab periphery was coated with a sheet of nylon to prevent any possible friction between the ingredients of the applied load and the inner surface of the steel box. This system of loading had caused the slab to fail in form of patterns which were satisfactory with the patterns adopted theoretically, as will be observed in the next articles.

A dial gauge of 50 mm maximum reading was used to measure the vertical deflection of the test slabs at centre for every increment of the applied loading. The procedure of loading and deflection measurement continued until excessive values of deflections were recorded indicating that the slab was on the verge of failure.

**Results Of The Ultimate Loads And Load-Deflection Relationships Of The Test Slabs.**

Table (2) contains the results of the experimental ultimate loads ($q_{u \ exp.}$) for the nine tested RC rectangular slabs together with their corresponding theoretical value ($q_{u \ theo.}$) obtained from the proposed elastic-plastic model by Abdul-Qader\cite{2}. For more information, the values of Johansen's\cite{1} collapse loads ($q_J$) for these slabs are also listed in the table and the load ratios
\[
\frac{q_{u \ exp.}}{q_J}, \quad \frac{q_{u \ theo.}}{q_J} \quad \text{and} \quad \frac{q_{u \ exp.}}{q_{u \ theo.}}
\]
for each test slab are calculated and shown for comparison. It can be seen that the proposed elastic-plastic model by Abdul-Qader\cite{2} can predict the ultimate load of any orthotropic RC rectangular slab having certain restraining conditions at the edges with a reasonable accuracy.

The complete load-deflection behaviour of a generalized uniformly loaded orthotropic RC rectangular slab as predicted by Abdul-Qader\cite{2} has also been examined. Figures (6) to (14) represent the theoretical and experimental load-deflection curves for the nine rectangular RC test slabs. In these figures, the horizontal straight line represents the value of Johansen's\cite{1} load. From these plots, the following conclusions may be drawn:

1- The load-deflection curves of the test slabs are found to be fairly comparable with the corresponding theoretical curves predicted by Abdul-Qader\cite{2}.
2- It is found that in all test slabs, there is a distinct reduction in the stiffness of the slab after initiation of cracking in the central region of the slab.
3- For an unrestrained RC slab ($S_1$), there is a continuous rise in the load-deflection curve beyond Johansen's\cite{1} load (post-yielding behaviour) which indicates that the slab can sustain higher load than Johansen's\cite{1} load at any large value of deflection.
4- For restrained RC slabs ($S_2$ to $S_9$), after the ultimate load has been reached the load decreases with further deflection owing to the reduction in the
compressive membrane forces. With more deflection the membrane forces in the central region of the slab change from compression to tension. At this stage, because of the large stretch of the slab surface, the cracks in the central region penetrate the whole thickness of the concrete and yielding of steel spreads throughout the region enabling the load to be carried by the reinforcement acting as a tensile membrane. With further deflection, the slab shows a recovery of load enhancement and such increase in load continues until the reinforcement starts to fracture.

Photos (9) to (17) show the cracking pattern of the tested slabs.

**Conclusions.**

Based on the results of the present study, several conclusions may be drawn. These may be summarized as follows:

1- The analysis shows that orthotropically reinforced concrete rectangular slabs having variably restrained edges can sustain loads more than those predicted by Johansen’s yield line theory.

2- The experimental ultimate load of the slab ($q_{ul, exp}$) is found to be greatest for RC rectangular slabs having all edges restrained against rotation and horizontal translation (i.e fixed). As the number of the restrained edges of the slab decreases the enhancement in the slab load will also decrease. It is when all the edges of the slab are unrestrained (i.e simply supported) that the initial collapse load of the slab will be the simple yield line theory load.

3- The theoretical elastic-plastic model presented recently by Abdul-Qader\(^{(2)}\) seems to compare reasonably with the experimental results of the present research.

**References**


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[17] ACI Committee 318, “Building Code Requirements for Structural Concrete (ACI-05) and Commentary-ACI 318M-05,” American Concrete Institute, Detroit, 2005.


### Table (1) Properties of the test slabs.

<table>
<thead>
<tr>
<th>Slab No.</th>
<th>Support Condition</th>
<th>Dimensions (mm)</th>
<th>$f_c$ MPa</th>
<th>$f_y$ MPa</th>
<th>Percentage of steel reinforcement ($\rho %$)</th>
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</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>$l_b \times l_a \times h$</td>
<td></td>
<td></td>
<td>$\rho_a^+$</td>
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<tr>
<td>S1</td>
<td>Case (1)</td>
<td>900<em>550</em>25</td>
<td>25.5</td>
<td>396</td>
<td>0.36</td>
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<tr>
<td>S2</td>
<td>Case (2)</td>
<td>900<em>550</em>25</td>
<td>27.1</td>
<td>396</td>
<td>0.36</td>
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<tr>
<td>S3</td>
<td>Case (3)</td>
<td>900<em>550</em>25</td>
<td>26.2</td>
<td>396</td>
<td>0.36</td>
</tr>
<tr>
<td>S4</td>
<td>Case (4)</td>
<td>900<em>550</em>25</td>
<td>25.8</td>
<td>396</td>
<td>0.36</td>
</tr>
<tr>
<td>S5</td>
<td>Case (5)</td>
<td>900<em>550</em>25</td>
<td>26.5</td>
<td>396</td>
<td>0.36</td>
</tr>
<tr>
<td>S6</td>
<td>Case (6)</td>
<td>900<em>550</em>25</td>
<td>25.2</td>
<td>396</td>
<td>0.36</td>
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<tr>
<td>S7</td>
<td>Case (7)</td>
<td>900<em>550</em>25</td>
<td>26.3</td>
<td>396</td>
<td>0.36</td>
</tr>
<tr>
<td>S8</td>
<td>Case (8)</td>
<td>900<em>550</em>25</td>
<td>27.4</td>
<td>396</td>
<td>0.36</td>
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<tr>
<td>S9</td>
<td>Case (9)</td>
<td>900<em>550</em>25</td>
<td>25.3</td>
<td>396</td>
<td>0.36</td>
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### Table (2) Comparison between the experimental and theoretical ultimate loads of the restrained test slabs.

<table>
<thead>
<tr>
<th>Slab No.</th>
<th>Support Condition</th>
<th>Experimental ultimate load ($q_u \exp.$) $kN/m^2$</th>
<th>Theoretical ultimate load ($q_u \text{theo.}$) $kN/m^2$</th>
<th>$q_u \exp.$</th>
<th>$q_u \text{theo.}$</th>
<th>$q_u \exp.$</th>
<th>$q_u \text{theo.}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>S1</td>
<td>Case (2)</td>
<td>75.52</td>
<td>95.67</td>
<td>50.35</td>
<td>1.50</td>
<td>1.9</td>
<td>0.79</td>
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<tr>
<td>S2</td>
<td>Case (3)</td>
<td>45.95</td>
<td>51.57</td>
<td>25.53</td>
<td>1.80</td>
<td>2.02</td>
<td>0.89</td>
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<tr>
<td>S3</td>
<td>Case (4)</td>
<td>60.29</td>
<td>70.02</td>
<td>31.4</td>
<td>1.92</td>
<td>2.23</td>
<td>0.86</td>
</tr>
<tr>
<td>S4</td>
<td>Case (5)</td>
<td>67.3</td>
<td>78.70</td>
<td>39.35</td>
<td>1.71</td>
<td>2.00</td>
<td>0.86</td>
</tr>
<tr>
<td>S5</td>
<td>Case (6)</td>
<td>49.09</td>
<td>53.94</td>
<td>26.97</td>
<td>1.82</td>
<td>2.00</td>
<td>0.91</td>
</tr>
<tr>
<td>S6</td>
<td>Case (7)</td>
<td>38.39</td>
<td>39.02</td>
<td>20.98</td>
<td>1.83</td>
<td>1.86</td>
<td>0.98</td>
</tr>
<tr>
<td>S7</td>
<td>Case (8)</td>
<td>63.4</td>
<td>77.07</td>
<td>36.7</td>
<td>1.73</td>
<td>2.10</td>
<td>0.82</td>
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<tr>
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<td>Case (9)</td>
<td>72.1</td>
<td>91.99</td>
<td>44.44</td>
<td>1.62</td>
<td>2.07</td>
<td>0.78</td>
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Figure (1) The nine possible cases of two-way rectangular slabs supported at all edges.

Photo (1) The tensile testing machine belonging to the laboratory of the Department of Minerals and Production Engineering in the University of Technology which has been used in the present study.
Figure (2) Idealized stress-strain relationship of 2.6 mm diameter steel wire.

Figure (3) The notations used for the steel ratios at different locations in the slab.

Photo (2) Details of the reinforcement mesh of slab $S_1$ (case1).
Photo (3) Details of the reinforcement mesh of slab $S_3$ (case3).

Photo (4) Details of the reinforcement mesh of slab $S_4$ (case 4).

Photo (5) Details of the reinforcement mesh of slab $S_6$ (case6).
Photo (6) Details of the reinforcement mesh of slab $S_7$ (case 7).

Photo (7) Details of the reinforcement mesh of slab $S_8$ (case 8).

Photo (8) A RC rectangular slab fixed along three edges while the fourth long edge is simply supported (slab case 8) in the test frame prior to testing. The details of section A-A are given in Figure (4).
Welding.

**Figure (4)** Details of section (A-A).

1. Rigid surrounding steel frame \((S \times 4.5)\)
2. Rigid steel column \((S \times 4.5)\)
3. Steel stiffeners (square section \(10^{\text{mm}} \times 10^{\text{mm}}\))
4. Steel plate (type A) (cross section \(150^{\text{mm}} \times 10^{\text{mm}}\))
5. Concrete slab model
6. Steel channel \((C \times 3 \times 6)\)
7. Steel plate (type B) (cross section \(60^{\text{mm}} \times 10^{\text{mm}}\))
8. \(12.7 \text{ mm} \) (1/2 in) diameter high-tensile screws at 100 mm center to center
9. \(12.7 \text{ mm} \) (1/2 in) diameter bright steel bolts at 333 mm \(\text{c/c}\) in long direction and 325 mm \(\text{c/c}\) in short direction

**Note:** Steel plate (type A) is drilled along their short and long direction with holes of \(15^{\text{mm}}\) diameter four holes in longer side and three holes in shorter side the benefit from these holes to connect slab with test frame by bolts when slab tests to give different boundary condition.
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Details of sec. (A-A) during test.

Figure (5) The System of loading used to represent uniform load.

Figure (6) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab simply supported at all edges (slab $S_1$).
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Figure (7) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed at all edges (slab $S_2$).

Figure (8) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed along the two short edges while the two long edges are simply supported (slab $S_3$).

Figure (9) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed along two adjacent edges while the other two edges are simply supported (slab $S_4$).
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Figure (10) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed along the two long edges while the two short edges are simply supported (slab $S_5$).

Figure (11) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed along one long edge while the remaining three edges are simply supported (slab $S_6$).

Figure (12) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab fixed along one short edge while the remaining three edges are simply supported (slab $S_7$).
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Figure (13) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab simply supported along one long edge while the remaining three edges are fixed (slab S8).

Figure (14) Theoretical and experimental load-deflection curve of an orthotropic RC rectangular slab simply supported along one short edge while the remaining three edges are fixed (slab S9).
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